### The Emergence of Reproducibility and Consistency in

**Diffusion Models** 

### Huijie Zhang

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October 28, 2023

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## Outline

## 1 Introduction

2 Reproducibility for Unconditional Diffusion Models

**3** Correlation between Reproducibility, Memorizability & Generalizability

**4** Reproducibility beyond Unconditional Diffusion Models

**5** Future Directions



• **Definition:** You can repeatedly run your algorithm on certain datasets and obtain the same (or similar) results on a particular project <sup>1</sup>.

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### • Very general in diffusion model

<sup>1</sup>similar to the definition uniquely identifiable encoding in  $[6, 7, 13, 20] \leftarrow 0$ 

• A powerfule generative model:

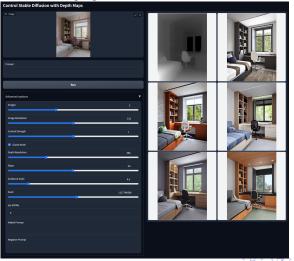
• Stable Diffusion [14]: Large text-to-image diffusion model

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'An epic painting of Gandalf the Black

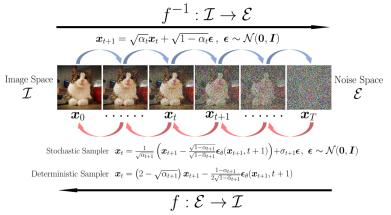
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- A powerfule generative model:
  - ControlNet [22]: Diffusion model with high flexiable guidance



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Definition: A generative model f : E → I mapping from the gaussian noise space E to the image manifold I



• **Training:** Only the denoiser function  $\epsilon_{\theta}$  requires training, following an easy pipeline:

Algorithm 1 Training

1: repeat

2: 
$$\mathbf{x}_0 \sim q(\mathbf{x}_0)$$

- 3:  $t \sim \text{Uniform}(\{1, \dots, T\})$
- 4:  $\boldsymbol{\epsilon} \sim \mathcal{N}(\mathbf{0}, \mathbf{I})$
- 5: Take gradient descent step on

$$\nabla_{\theta} \left\| \boldsymbol{\epsilon} - \boldsymbol{\epsilon}_{\theta} (\sqrt{\bar{lpha}_t} \mathbf{x}_0 + \sqrt{1 - \bar{lpha}_t} \boldsymbol{\epsilon}, t) \right\|^2$$

6: until converged

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# Samples Visualization

**Q1:** Starting from the **same noise input**, how are the generated data samples from various diffusion models related to each other?

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(a) DDPMv4

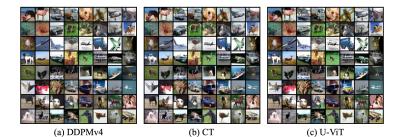
(b) CT

(c) U-ViT

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## Samples Visualization

**Q1:** Starting from the **same noise input**, how are the generated data samples from various diffusion models related to each other?



Training on the same dataset, sampling by a deterministic sampler.

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# Quantitative analysis

• **Metric**: We define *reproducibility (RP) score* to measure the this phenomenon:

 $\mathsf{RP Score} \ := \ \mathbb{P}\left(\mathcal{M}_{\mathsf{SSCD}}(\boldsymbol{x}_1, \boldsymbol{x}_2) > 0.6\right),$ 

represents the *probability* of a generated sample pair  $(x_1, x_2)$  from two different diffusion models to have *self-supervised copy detection* (SSCD) similarity  $\mathcal{M}_{\text{SSCD}}$  larger than 0.6. We sampled 10K noise to estimate the probability. The SSCD similarity is first introduced in [12] to measure the replication between image pair  $(x_1, x_2)$ , which is defined as the following:

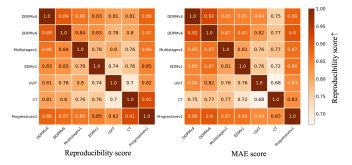
$$\mathcal{M}_{\mathsf{SSCD}}(\boldsymbol{x}_1, \boldsymbol{x}_2) = rac{\mathsf{SSCD}(\boldsymbol{x}_1) \cdot \mathsf{SSCD}(\boldsymbol{x}_2)}{||\mathsf{SSCD}(\boldsymbol{x}_1)||_2 \cdot ||\mathsf{SSCD}(\boldsymbol{x}_2)||_2}$$

where  $\mathsf{SSCD}(\cdot)$  represents a neural descriptor for copy detection.

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# Quantitative analysis

• Results:



**C2:** Diffusion models consistently generate **nearly identical contents**, irrespective of network architectures, training and sampling procedures, and perturbation kernels.

# Mapping from Noise Hyperplane to Image Manifold

#### Results:



DDPMv6



Multistagev1

Pick three initial noises  $(\epsilon_1, \epsilon_2, \epsilon_3)$  to generate clear images  $(x_1, x_2, x_3)$  in the image manifold  $\mathcal{I}$ . Second, we create a 2D noise hyperplane with  $\epsilon(\alpha, \beta) = \alpha \cdot (\epsilon_2 - \epsilon_1) + \beta \cdot (\epsilon_3 - \epsilon_1) + \epsilon_1$ . And utilize them to generate images  $x(\alpha, \beta)$ , and RP Score  $:= max_{k \in \{1,2,3\}}[\mathcal{M}_{\text{SSCD}}(x_k, x(\alpha, \beta))]$ 

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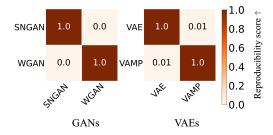
- Similar unique encoding maps across different network architectures.
- Local Lipschitzness of the unique encoding from noise to image space.

## Reproducibility for other generative models

• **Question**: Dose model reproducibility appear to other generative models?

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Conclusion: Reproducibility doesn't appear for GAN and general VAE;

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### 2 Reproducibility for Unconditional Diffusion Models

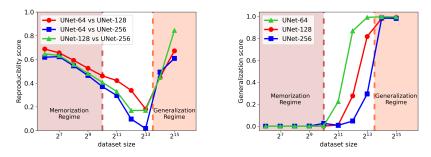
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#### Generalizability

## "Memorization" and "Generalization" regimes



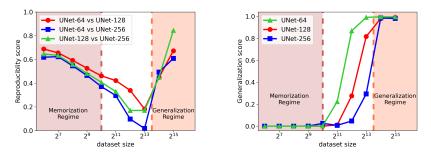
generalization (GL) score :=  $1 - \mathbb{P}\left(\max_{i \in [N]} [\mathcal{M}_{SSCD}(\boldsymbol{x}, \boldsymbol{y}_i)] > 0.6\right)$  between the generated sample  $\boldsymbol{x}$  and all samples from training dataset  $\{\boldsymbol{y}_i\}_{i=1}^N$ .

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#### Generalizability

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**C3:** The reproducibility of diffusion models manifests in two distinct training regimes, both **strongly correlated** with the model's generalizability.

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# Theory for reproducibility in Memorization Regime

#### Theorem (1)

Suppose we train a diffusion model denoiser function  $\epsilon_{\theta}(x,t)$  with parameter  $\theta$  on a training dataset  $\{y_i\}_{i=1}^N$  of N-samples, by minimizing the training loss

$$\min_{\boldsymbol{\theta}} \mathcal{L}(\boldsymbol{\epsilon}_{\boldsymbol{\theta}}; t) = \mathbb{E}_{\boldsymbol{x}_0 \sim p_{data}(\boldsymbol{x})} \mathbb{E}_{\boldsymbol{x} \sim p_t(\boldsymbol{x}|\boldsymbol{x}_0)} [||\boldsymbol{\epsilon} - \boldsymbol{\epsilon}_{\boldsymbol{\theta}}(\boldsymbol{x}, t)||^2],$$
(1)

assuming data  $x_0$  follows a multi-delta distribution  $p_{\text{data}}(x) = \frac{1}{N} \sum_{i=1}^N \delta(x - y_i)$ , and the perturbation kernel  $p_t(x_t | x_0) = \mathcal{N}(x_t; s_t x_0, s_t^2 \sigma_t^2 \mathbf{I})$  with parameters  $s_t, \sigma_t$ . Then we show the optimal denoiser  $\epsilon_{\theta}^*(x; t) = \arg \min_{\epsilon_{\theta}} \mathcal{L}(\epsilon_{\theta}; t)$  is:

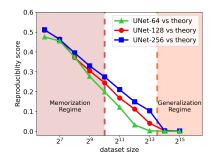
$$\boldsymbol{\epsilon}_{\boldsymbol{\theta}}^{*}(\boldsymbol{x};t) = \frac{1}{s_{t}\sigma_{t}} \left[ \boldsymbol{x} - s_{t} \frac{\sum_{i=1}^{N} \mathcal{N}(\boldsymbol{x};s_{t}\boldsymbol{y}_{i},s_{t}^{2}\sigma_{t}^{2}\mathbf{I})\boldsymbol{y}_{i}}{\sum_{i=1}^{N} \mathcal{N}(\boldsymbol{x};s_{t}\boldsymbol{y}_{i},s_{t}^{2}\sigma_{t}^{2}\mathbf{I})} \right].$$
(2)

Moreover, suppose a trained diffusion model could converge to the optimal denoiser  $\epsilon^*_{\theta}(\boldsymbol{x};t)$  and we use a deterministic ODE sampler to generate images using  $\epsilon^*_{\theta}(\boldsymbol{x};t)$ , then  $f: \mathcal{E} \mapsto \mathcal{I}$ , which is determined by the  $\epsilon^*_{\theta}(\boldsymbol{x};t)$  and the ODE sampler, is an invertiable mapping and the inverse mapping  $f^{-1}$  is a unique identifiable encoding.

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# Experimental verification of Theorem (1)

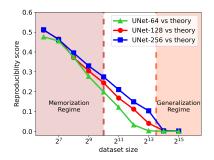
• Reproducibility score between theoretical results and experimental results.



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# Experimental verification of Theorem (1)

• Reproducibility score between theoretical results and experimental results.



• **Conclusion**: Diffusion model could converge to the theoretical solution when model capacity is enough.

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## More than unconditional diffusion model

**C4:** Model reproducibility holds **more generally** across conditional diffusion models, diffusion models for inverse problems, the fine-tuning of diffusion models.

## Intro to conditional diffusion model

• Enable conditional generation, e.g. class condition, text-to-image, image-to-image translation.[14].

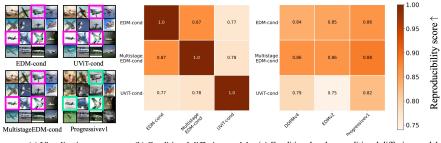
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- Utilize  $\epsilon_{\theta}(\boldsymbol{x}_t, t, c)$  for both training and sampling.

## Reproducibility of conditional diffusion model



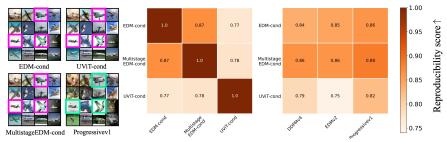
(a) Visualization

(b) Conditional diffusion models (c) Conditional and unconditional diffusion models

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## Reproducibility of conditional diffusion model

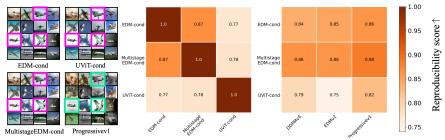


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 $\begin{aligned} \mathsf{RP}_{cond} \ \mathsf{Score} &:= \mathbb{P}\left(\mathcal{M}_{\mathsf{SSCD}}(\boldsymbol{x}_1^c, \boldsymbol{x}_2^c) > 0.6 \mid c \in \mathcal{C}\right), \ (\boldsymbol{x}_1^c, \boldsymbol{x}_2^c) \ \text{are generated by two} \\ \text{conditional models from the same initial noise and conditioned on the class} \ c \in \mathcal{C} \\ \mathsf{RP}_{between} \ \mathsf{Score} &:= \mathbb{P}\left(\max_{c \in \mathcal{C}} \left[\mathcal{M}_{\mathsf{SSCD}}(\boldsymbol{x}_1, \boldsymbol{x}_2^c)\right] > 0.6\right), \ \text{for an unconditional generation} \ \boldsymbol{x}_1 \ \text{and conditional generation} \ \boldsymbol{x}_2^c \ \text{starting from the same noise.} \end{aligned}$ 

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Model reproducibility of conditional models is evident and linked with unconditional counterparts.

- Inverse problem: reconstruct an unknown signal u from the measurements z of the form z = A(u) + η, where A denotes some (given) sensing operator and η is the noise.
- Enable conditional generation with only pre-trained unconditional denoiser  $\epsilon_{\theta}(x_t,t)$

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   x<sub>t</sub> ← x<sub>t</sub> ξ<sub>t</sub>∇<sub>x<sub>t</sub></sub> ||u A(x̂<sub>0</sub>) ||<sup>2</sup><sub>2</sub>

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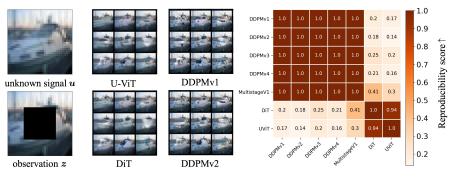
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  abla_{oldsymbol{x}_t} ||oldsymbol{u} \mathcal{A}\left(\hat{oldsymbol{x}}_0
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- Diffusion Posterior Sampling (DPS) [1]



# Reproducibility of diffusion model for inverse problem

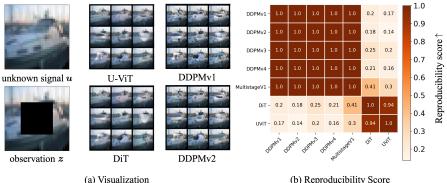


(b) Reproducibility Score

(a) Visualization

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# Reproducibility of diffusion model for inverse problem



(b) Reproducibility Score

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Model reproducibility largely holds only within the same type of network architectures.

# Intro to diffusion model fine-tuning

• Pre-trained large diffusion model (e.g. stable diffusion), fine-tuning only part of the diffusion model (e.g. attention layer, txt embedding.) and on few-shot images.

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- Pre-trained large diffusion model (e.g. stable diffusion), fine-tuning only part of the diffusion model (e.g. attention layer, txt embedding.) and on few-shot images.
- Obtain incredible generalizability, e.g. DreamBooth [15].



Input images



in the Acropolis



sleeping





getting a haircut

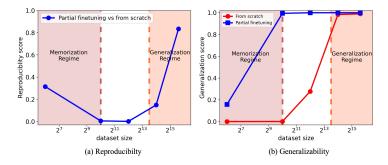


in a doghouse in a bucket

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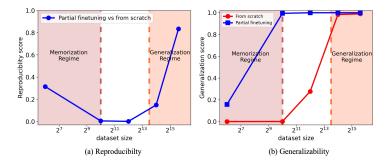
#### Reproducibility of diffusion model fine-tuning



Pretrained on CIFAR-100, fine-tuning on CIFAR-10. Only fine-tuning the attention layer.

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Partial fine-tuning reduces reproducibility but improves generalizability in "memorization regime".

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  - Analyzing the generalizability of diffusion models [21].
  - Connection between diffusion models and the Schrödinger bridge [16, 3, 11, 4, 9, 8] (an optimal transport problem).

# Q & A

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